

# 机器学习 在材料设计中的应用

# The Story of Light Bulb



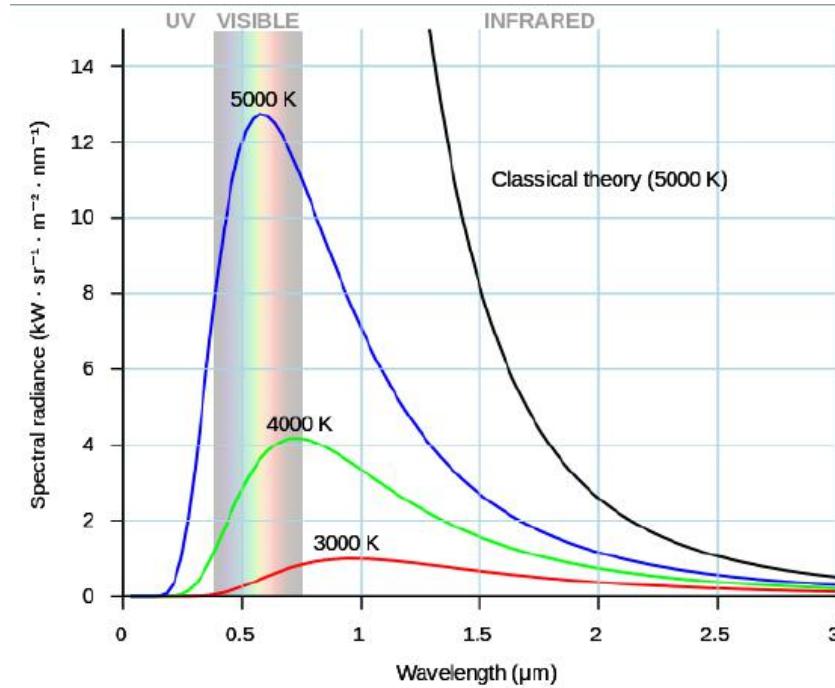
6000+ materials have been tested

# The Story of Light Bulb



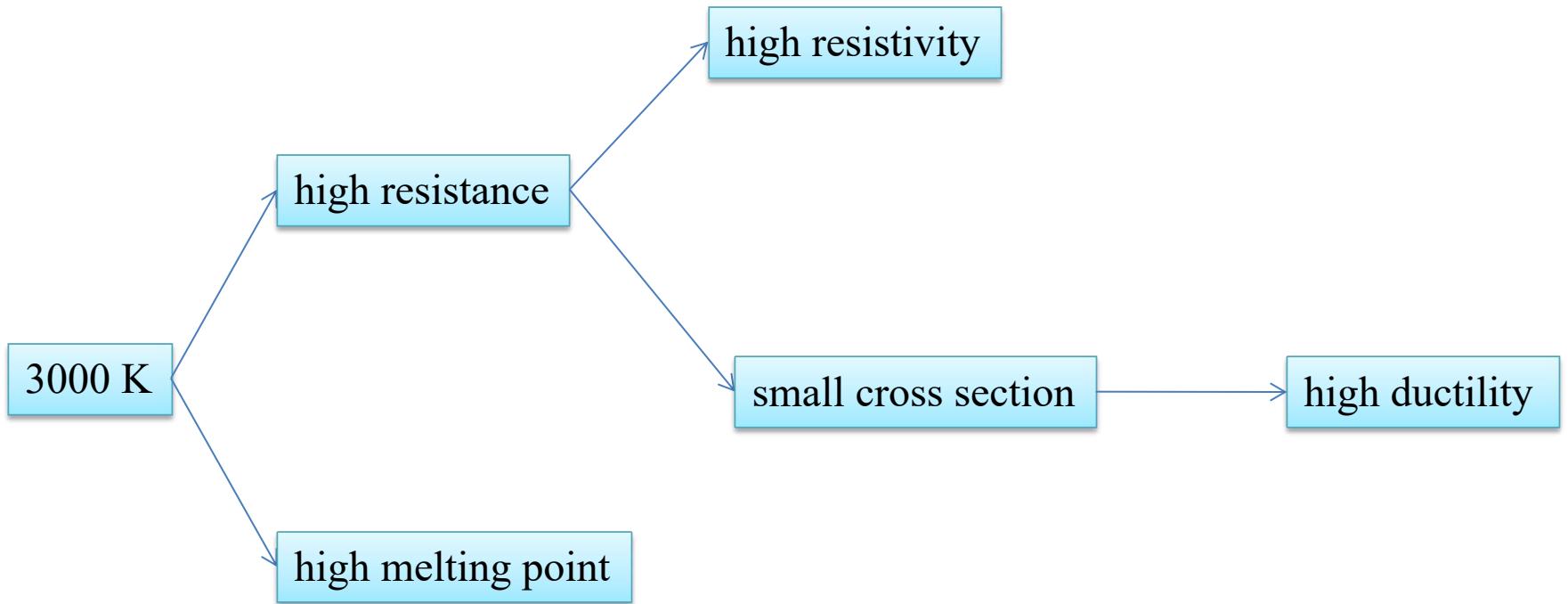
Among numerous experiments, Edison's team finally discovered that carbonized bamboo filament could last over 1,200 hours.

# Physics: black body radiation

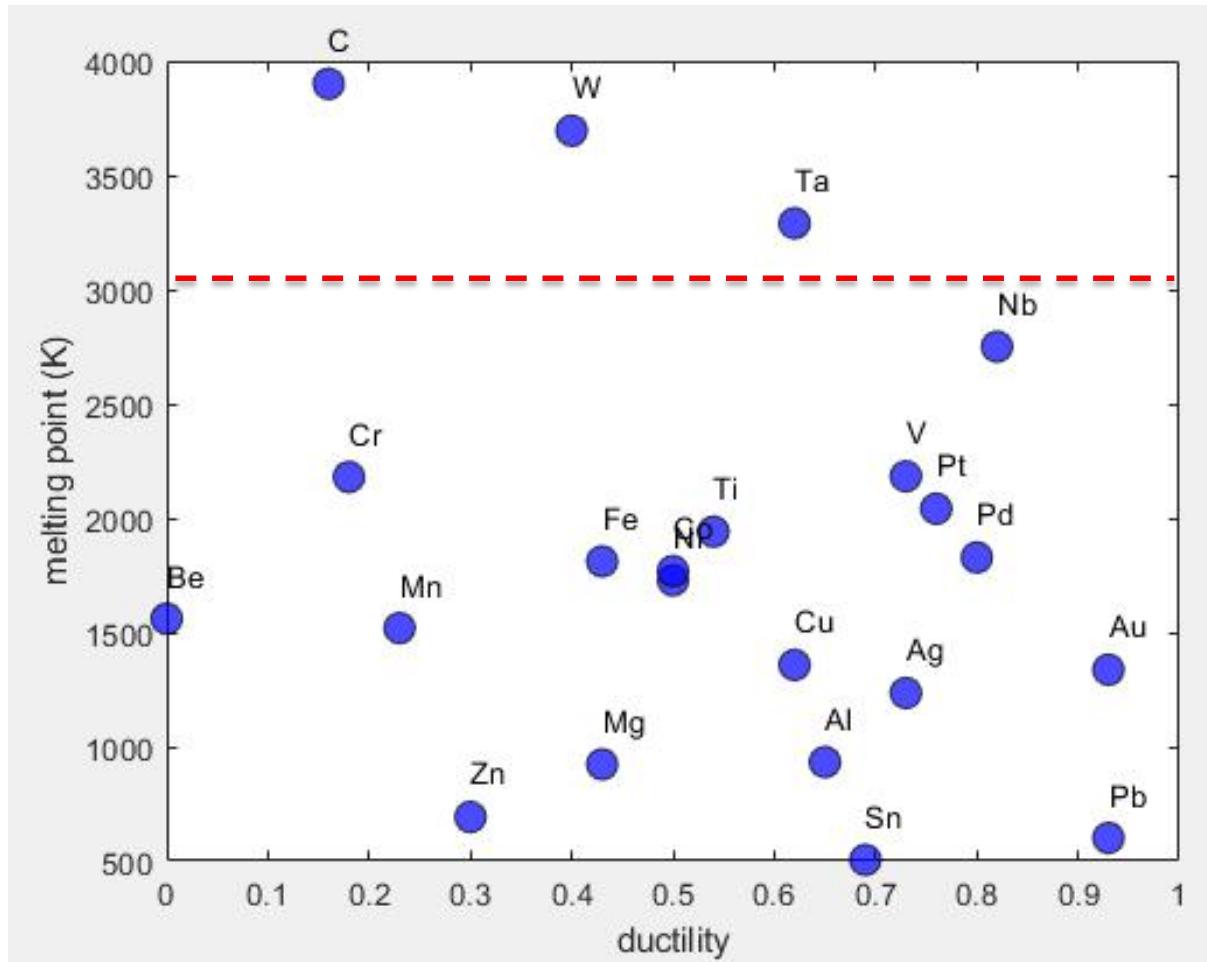


$$B(\nu, T) = \frac{2h\nu^3}{c^2} \frac{1}{e^{\frac{h\nu}{k_B T}} - 1}$$

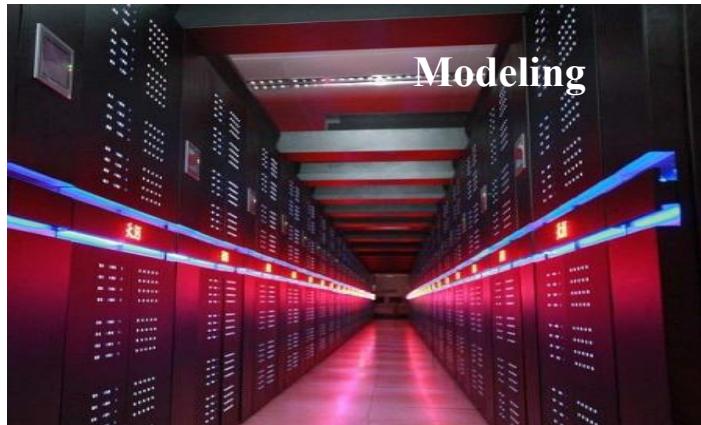
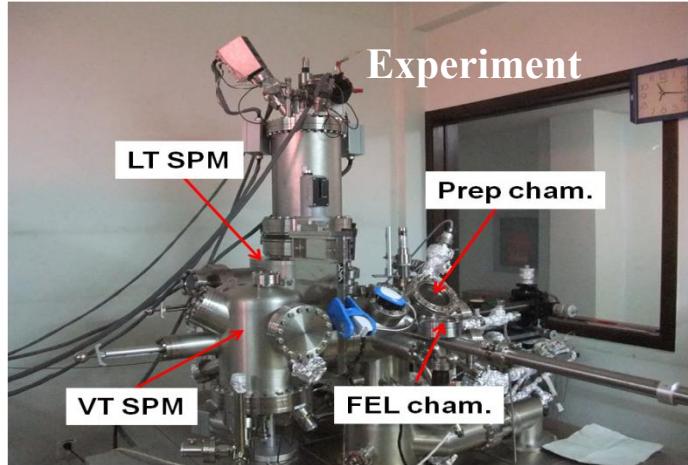
# Melting point and ductility



# Melting point and ductility



# Material Informatics



$$\begin{aligned}
 \lambda &= \frac{h}{\sqrt{2eUm_e}} \quad \ell_c = \ell_0(1+d\Delta t) \quad \vec{\ell} = \frac{c_0}{R+R_i} \vec{\omega} \sin(\omega_c t + \phi) \vec{y} \\
 f_0 &= \frac{1}{2\pi} \frac{\int_{\vec{S}} Y_{00}}{\int_{\vec{C}}} \quad Y_{00} = \frac{1}{2/L} \sin \frac{n\pi x}{L} \\
 \mu \vec{B} d\vec{l} &= \mu \iint \vec{J} d\vec{S} \quad \vec{S} = \frac{1}{2} (\vec{E} \times \vec{B}) \\
 C(S) &= \frac{\sqrt{3kT}}{m_e} = \frac{\sqrt{3kT N_A}}{M_m} = \frac{\sqrt{3kT}}{M_m \cdot 10^3} \\
 V_0 &= \frac{\sqrt{3kT}}{m_e} = \frac{\sqrt{3kT N_A}}{M_m} = \frac{\sqrt{3kT}}{M_m \cdot 10^3} \\
 E &= \frac{\hbar k^2}{r} 1 \text{ pc} = \frac{1 \text{ AU}}{r} \iint \vec{B} d\vec{S} = Q^* \\
 \lambda &= \frac{\ell n_2}{F_h} \quad F_h = Shpg \quad f_0 = \frac{1}{2m} \quad M = \vec{F} d\cos\alpha \\
 \left(\frac{E_0}{E_0}\right) &= \frac{2\omega_S \vec{v}_0 \cos\theta_0^2}{\cos(\theta_0 - \theta_0^2) \sin(\theta_0 + \theta_0^2)} \quad \vec{f}_0 = \frac{1}{2\pi} \frac{\vec{C} \vec{L}}{\int_{\vec{C}} \vec{E} d\vec{l}} \quad \vec{S} \vec{I}_m = \int_{\vec{C}} \left[ \frac{1}{\vec{E}^2} + \left( \frac{1}{X_C} - \frac{1}{X_L} \right)^2 \right] \lambda^* T = b \\
 \vec{E}_0 &= \vec{E}_0 \sin(\theta_0 + \theta_0^2) \\
 R &= R_0 \frac{3/A}{C(L)} \quad \int_{\vec{C}} \vec{E} d\vec{l} = -\int_{\vec{C}} \vec{B} d\vec{S} \quad p = \frac{1}{\vec{E}^2} - \frac{1}{X_C^2} - \frac{1}{X_L^2} \\
 S &= \frac{1}{A} \frac{\partial \omega}{\partial t} \quad \int_{\vec{C}} \vec{H} d\vec{l} = \iint \left( \vec{J} + \frac{\partial \vec{B}}{\partial t} \right) \cdot d\vec{S} \quad Q = m C \Delta t \quad F_g = \rho g \frac{M_0 M_1}{r^2} \\
 W &= F_g \cdot \cos\omega \quad \vec{f}_0 = \frac{1}{2\pi} \frac{\vec{C} \vec{L}}{\int_{\vec{C}} \vec{E} d\vec{l}} \quad \vec{P} = U \vec{I} \quad h = \frac{1}{2} \vec{g}^2 V - V_0(t + \beta \Delta t) \\
 C &= \frac{\rho \omega_{max}^2 + \vec{g}^2}{(n+1)^2 + \vec{g}^2} \quad \vec{f}_0 = \frac{\rho \omega_{max}^2}{(n+1)(\vec{g}^2 - \vec{g}_0^2)} \quad \nabla_x \left( \frac{\partial \vec{g}}{\partial t} \right) = -\mu_0 \frac{\partial}{\partial t} \left( \frac{\partial \vec{B}}{\partial t} \right) = \epsilon_0 \mu_0 \frac{\partial^2 \vec{E}}{\partial t^2}
 \end{aligned}$$



**Material Informatics=Materials Science + Data Science**

# Advantages

**Although the data-driven approach is internally related to other approaches, it has unique features and advantages:**

- **Enlarge the search space**
- **Have a global vision**
- **Find hidden patterns**

# Enlarge the search space

**Human:** Thomas Edison did thousands of experiments before finding an acceptable materials for the filament of electric bulb



10<sup>3</sup>

**MI:** About 200,000 experimentally realized materials are documented in Inorganic Crystal Structure Database



FIZ Karlsruhe

**ICSD**

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**About ICSD**

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► Publications

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► ICSD Web

► ICSD Desktop

► ICSD Intranet

► ICSD Demo Version

**Customer Support**

► Price List

**ICSD Web**

ICSD Web is a host-based internet solution for institutions that would like to reduce their TCO, while at the same time offering their users easy-to-use, highly efficient web access to the database.

The ICSD Web login page can be found [here](#).

At present, the ICSD contains more than 193,000 entries, including

- 2,522 crystal structures of the elements
- 38,659 records for binary compounds
- 70,881 records for ternary compounds
- 69,900 records for quaternary and quintenary compounds
- About 154,000 entries (80%) have been assigned a structure type.

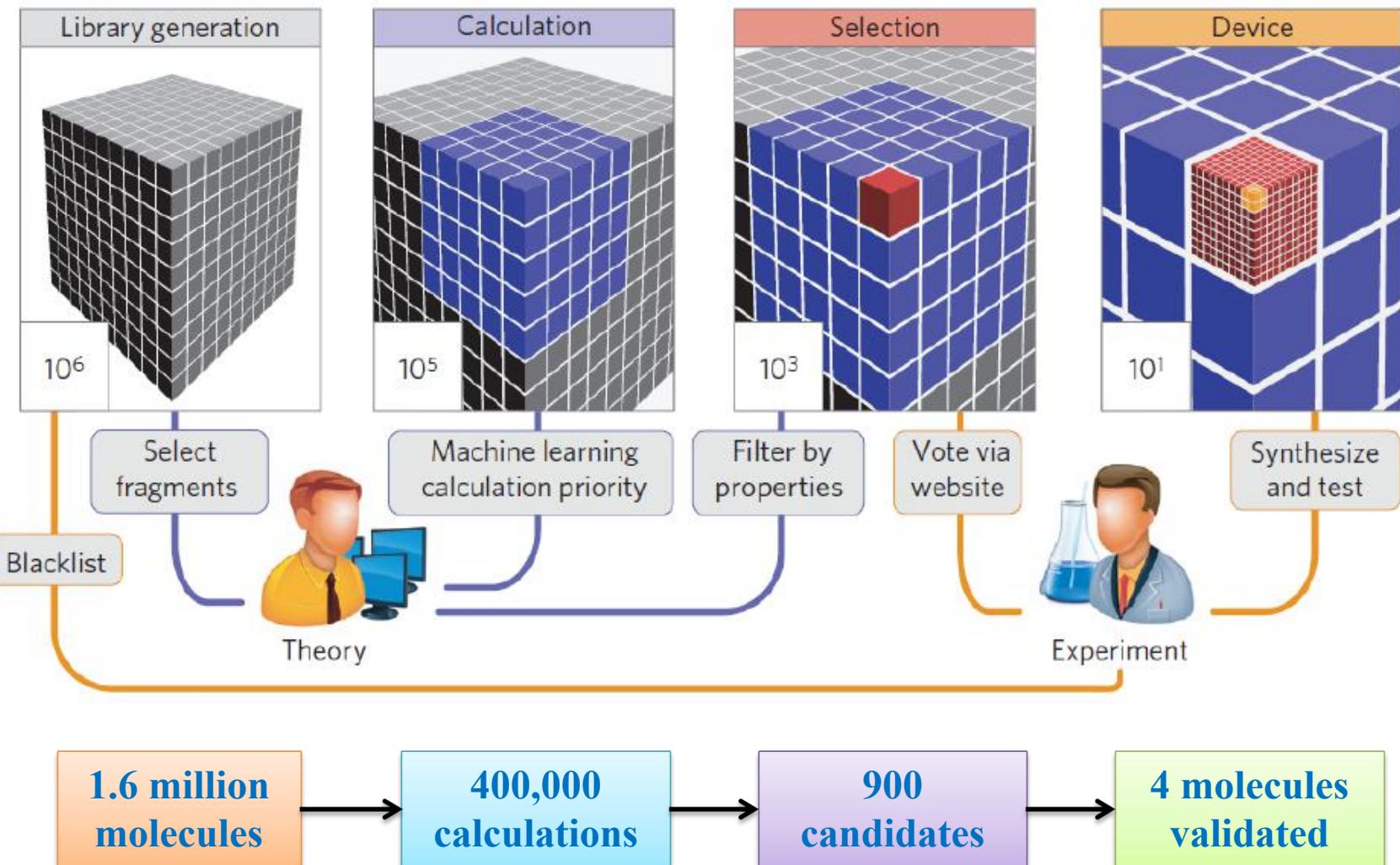
There are currently 9,004 structure prototypes.

Detailed information on the ICSD may be found in the [scientific manual](#).

105

# OLED molecule design

Nature Mater. 15, 1120 (2016)

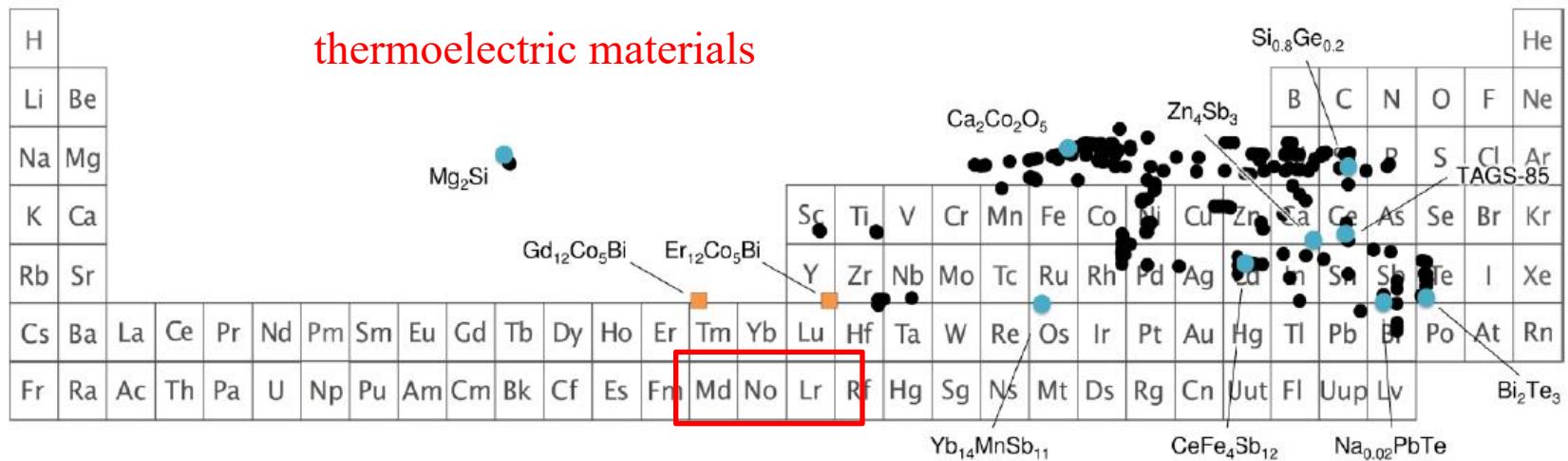


# Have a global vision

053213-2

Gaultois *et al.*

APL Mater. 4, 053213 (2016)



**Human:** Researchers tend to improve properties of known materials (nano-structuring, doping etc) or make substitution in known structures.

**MI:** Recommendation engines have no bias toward any material class, hence more likely to identify new materials.

# Three key components

Experimental Data or Computational Data

Data

Algorithm

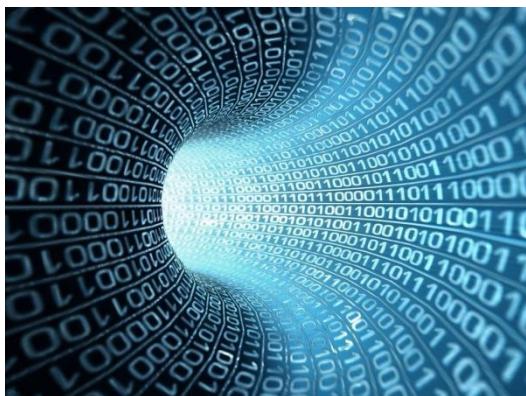
MI

Knowledge

Machine  
Learning  
Algorithms

Knowledge in  
Materials Science

# Data Resources



Experimental data (e.g., x-ray diffraction)

Computational data (e.g., VASP, Qchem)

Database

[Materials Project](#)

[COD](#)

[ICSD](#)

AFLOWLIB

OQMD

Mat Navi

NoMaD

MMDB

CATAPP

MAGNDATA

# Materials Project

The screenshot shows the Materials Project website with a dark blue background featuring a hexagonal lattice pattern. At the top, there is a navigation bar with links: Home, About ▾, Apps ▾, Documentation ▾, API, and Login. The 'Login' button is highlighted with a red border. Below the navigation bar, a large text block describes the project's mission: "Harnessing the power of supercomputing and state of the art electronic structure methods, the Materials Project provides open web-based access to computed information on known and predicted materials as well as powerful analysis tools to inspire and design novel materials." At the bottom left, there are two buttons: a teal one labeled "Learn more" and a red one labeled "YouTube Tutorials". To the right, there is a call-to-action button with a teal border containing the text "Sign In or Register" and "to start using".

Harnessing the power of supercomputing and state of the art electronic structure methods, the Materials Project provides open web-based access to computed information on known and predicted materials as well as powerful analysis tools to inspire and design novel materials.

Learn more

YouTube Tutorials

Sign In or Register to start using

注册一个Materials Project账号并登陆

<https://www.materialsproject.org/>

# Materials Project

Home   About ▾   Apps ▾   Documentation ▾   API    Tutorial

Explore Materials   Advanced Search Syntax

1	H	2	He																																
3	Li	4	Be																																
11	Na	12	Mg																																
19	K	20	Ca	21	Sc	22	Ti	23	V	24	Cr	25	Mn	26	Fe	27	Co	28	Ni	29	Cu	30	Zn	31	Ga	32	Ge	33	As	34	Se	35	Br	36	Kr
37	Rb	38	Sr	39	Y	40	Zr	41	Nb	42	Mo	43	Tc	44	Ru	45	Rh	46	Pd	47	Ag	48	Cd	49	In	50	Sn	51	Sb	52	Te	53	I	54	Xe
55	Cs	56	Ba	57-71	La-Lu	72	Hf	73	Ta	74	W	75	Re	76	Os	77	Ir	78	Pt	79	Au	80	Hg	81	Tl	82	Pb	83	Bi	84	Po	85	At	86	Rn
87	Fr	88	Ra	89-103	Ac-Lr	104	Rf	105	Db	106	Sg	107	Bh	108	Hs	109	Mt	110	Ds	111	Rg	112	Cn												
57	La	58	Ce	59	Pr	60	Nd	61	Pm	62	Sm	63	Eu	64	Gd	65	Tb	66	Dy	67	Ho	68	Er	69	Tm	70	Yb	71	Lu						
89	Ac	90	Th	91	Pa	92	U	93	Np	94	Pu	95	Am	96	Cm	97	Bk	98	Cf	99	Es	100	Fm	101	Md	102	No	103	Lr						

# of elements  
e.g., 4 or >2 & <6

excluded elements  
Cl Br

Submit

Material Tags  
imgreite

Band Gap (eV)  
0      10

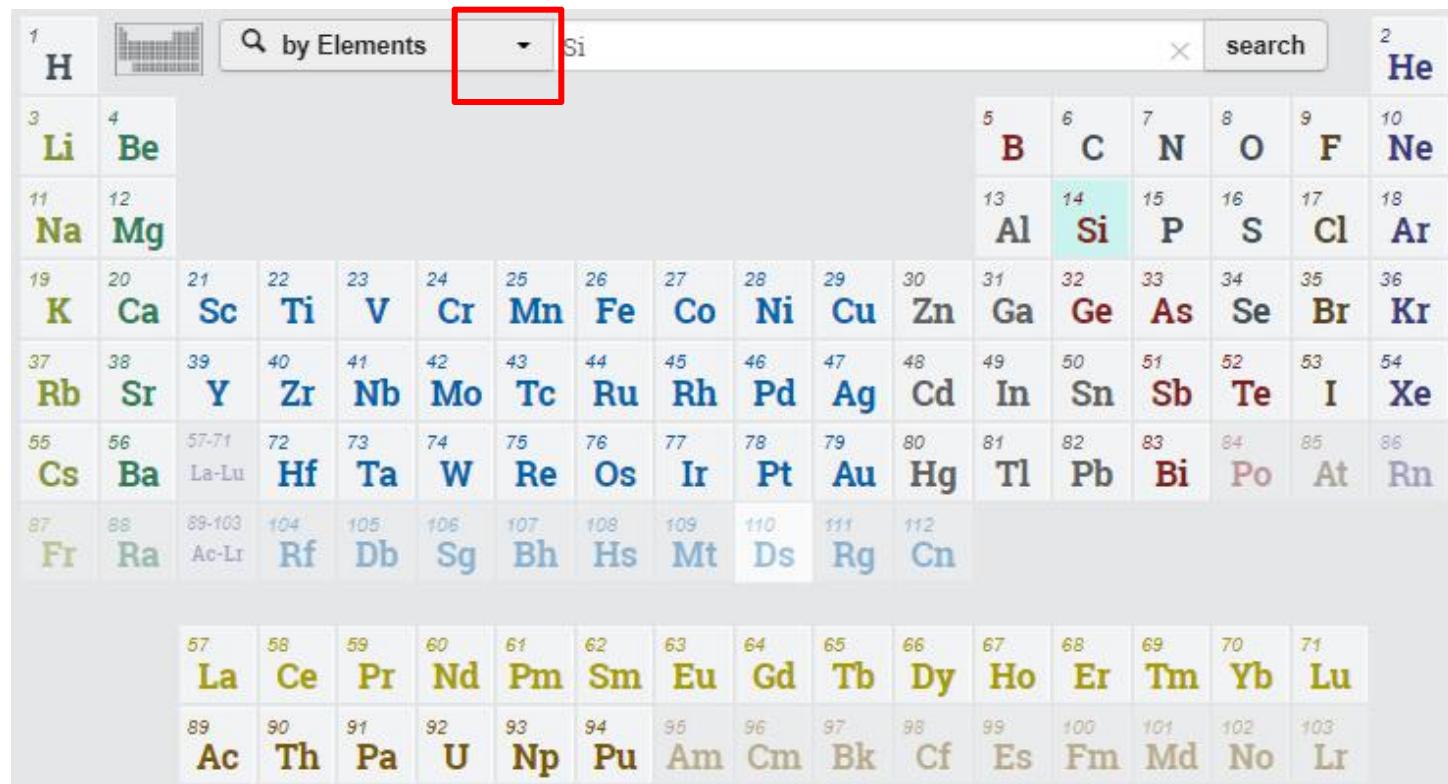
Energy Above Hull  
0      6

Formation Energy  
-4      4

# 材料领域的机器学习

## 如何获取数据--推荐的几个数据库

搜索得到  
Si的结构  
、能带和  
态密度  
DOS



The screenshot shows a periodic table search interface. At the top, there is a search bar labeled "by Elements" with a dropdown arrow, which is highlighted with a red box. The search term "Si" is entered into the search bar. Below the search bar, the periodic table is displayed with various elements highlighted in different colors. The element Silicon (Si) is highlighted in light blue. Other elements like Hydrogen (H), Helium (He), Carbon (C), Nitrogen (N), Oxygen (O), Fluorine (F), and Neon (Ne) are also highlighted in different colors. The rest of the elements are shown in their standard black font.

1	H		<input type="text" value="by Elements"/>	<input type="button" value="▼"/>	Si	<input type="button" value="X"/>	<input type="text" value="search"/>	2	He
3	Li	4 Be						5	B
11	Na	12 Mg						6	C
19	K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co
37	Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh
55	Cs	56 Ba	57-71 La-Lu	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir
87	Fr	88 Ra	89-103 Ac-Lr	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt
									110 Ds
									111 Rg
									112 Cn
57	La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb
89	Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk
									98 Cf
									99 Es
									100 Fm
									101 Md
									102 No
									103 Lr

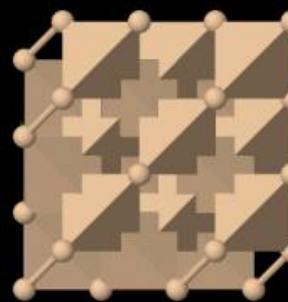
# Search Materials

Materials Id	Formula	Spacegroup	Formation Energy (eV)	E Above Hull (eV)	Band Gap (eV)	Nsites	Density (gm/cc)	Volume	
mp-149	Si	Fd3m	0	0	0.612	2	2.281	40.888	<input type="checkbox"/>
mp-165	Si	P6 <sub>3</sub> /mmc	0.011						

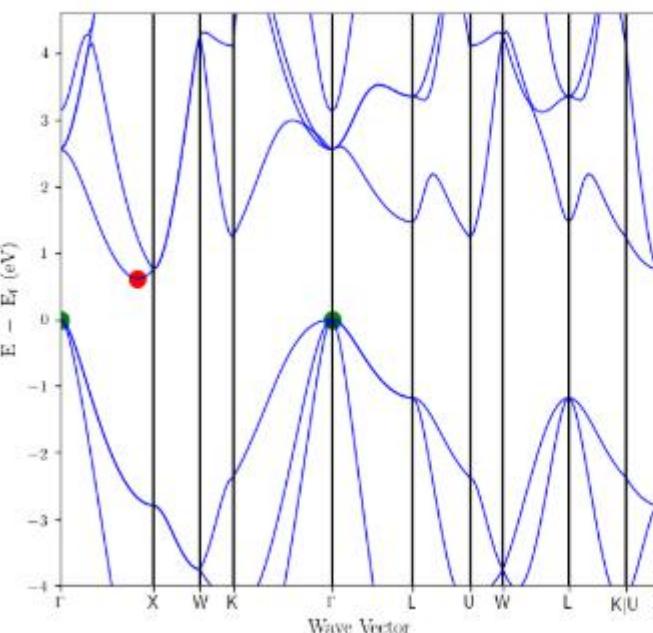
MATERIAL ID: DOI:  
Si mp-149 10.17188/1190959 

[Electronic Structure](#) [Phonon Dispersion](#) [X-Ray Diffraction](#) [X-Ray Absorption](#) [Substrates](#)  
[Calculation Summary](#) [Provenance/Citation](#)

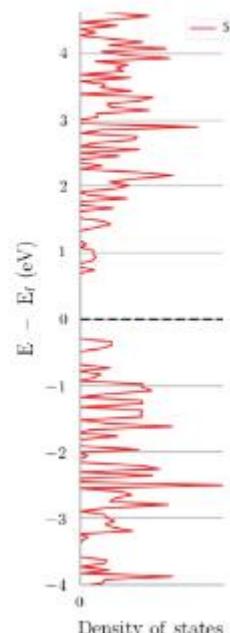
HM: F 1  
 $a=5.469\text{\AA}$   
 $b=5.469\text{\AA}$   
 $c=5.469\text{\AA}$   
 $\alpha=90.000^\circ$   
 $\beta=90.000^\circ$   
 $\gamma=90.000^\circ$



Band Structure



Density of States



Band Gap: 0.612 eV

Structure Type: Conventional Standard Primitive Refined 

# 材料领域的机器学习—练习

任务：

mp-66和mp-48哪个是金刚石哪个是石墨，哪种更稳定？

石墨:mp-48, 0.000 eV formation energy/atom,  
P6<sub>3</sub>/mmc

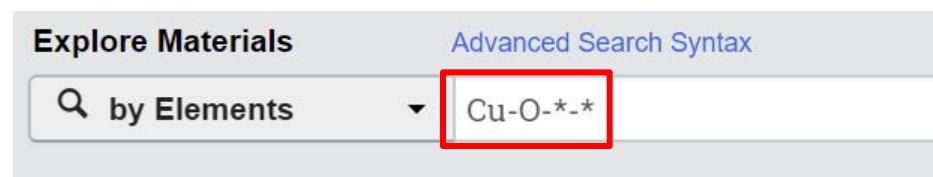
金刚石:mp-66, 0.134 eV formation  
energy/atom, Fd-3m

比较MoS<sub>2</sub>和MoSe<sub>2</sub>的带隙？哪个更宽？

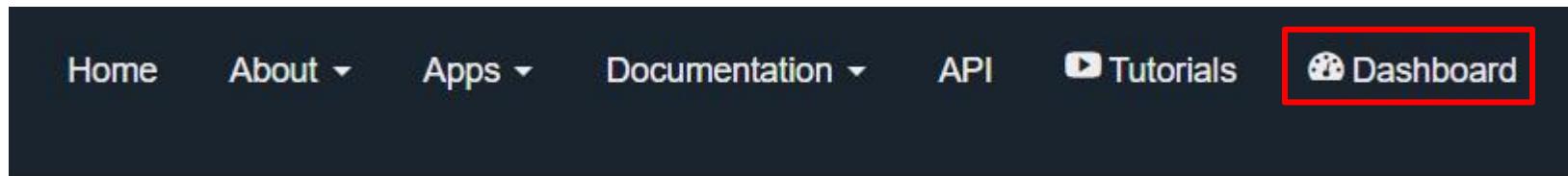
MoS<sub>2</sub>:mp-1434 Eg=1.204 eV

MoSe<sub>2</sub>:mp-1027692 Eg=1.138 eV

搜索含Cu, O的四元素化合物



# 材料领域的机器学习



# 材料领域的机器学习

查看材料信息：

[https://www.materialsproject.org/rest/v2/materials/mp-24972/vasp/?API\\_KEY=ue01GUMslBL9JRIH](https://www.materialsproject.org/rest/v2/materials/mp-24972/vasp/?API_KEY=ue01GUMslBL9JRIH)

查看材料能带信息：

[https://www.materialsproject.org/rest/v2/materials/mp-24972/vasp/bandstructure?API\\_KEY=ue01GUMslBL9JRIH](https://www.materialsproject.org/rest/v2/materials/mp-24972/vasp/bandstructure?API_KEY=ue01GUMslBL9JRIH)

查看材料态密度信息：

[https://www.materialsproject.org/rest/v2/materials/mp-24972/vasp/dos?API\\_KEY=ue01GUMslBL9JRIH](https://www.materialsproject.org/rest/v2/materials/mp-24972/vasp/dos?API_KEY=ue01GUMslBL9JRIH)

查看材料结构信息：

[https://www.materialsproject.org/rest/v2/materials/mp-24972/vasp/structure?API\\_KEY=ue01GUMslBL9JRIH](https://www.materialsproject.org/rest/v2/materials/mp-24972/vasp/structure?API_KEY=ue01GUMslBL9JRIH)

# 材料领域的机器学习

## **elasticity**

Mechanical properties in the elastic limit. Contains the full elastic tensor as well as derived properties, e.g. Poisson ratio and bulk (K) and shear (G) moduli. Consult our [hierarchical documentation](#) for the particular names of sub-keys.

## **piezo**

Piezoelectric properties. Contains a tensor and derived properties. Again, consult our [repository](#) for the names of sub-keys.

## **diel**

Dielectric properties. Contains a tensor (one each for total and electronic contribution) and derived properties, e.g. dielectric constant, refractive index, and recognized potential for ferroelectricity.

## *Calculation parameters*

### **is\_hubbard**

A boolean indicating whether the structure was calculated using the Hubbard U extension to DFT

### **hubbards**

An array of Hubbard U values, where applicable.

### **is\_compatible**

Whether this calculation is considered compatible under the GGA/GGA+U mixing scheme.

## *Electronic structure*

### **band\_gap**

The calculated band gap

### **dos**

The calculated density of states in the pymatgen json representation

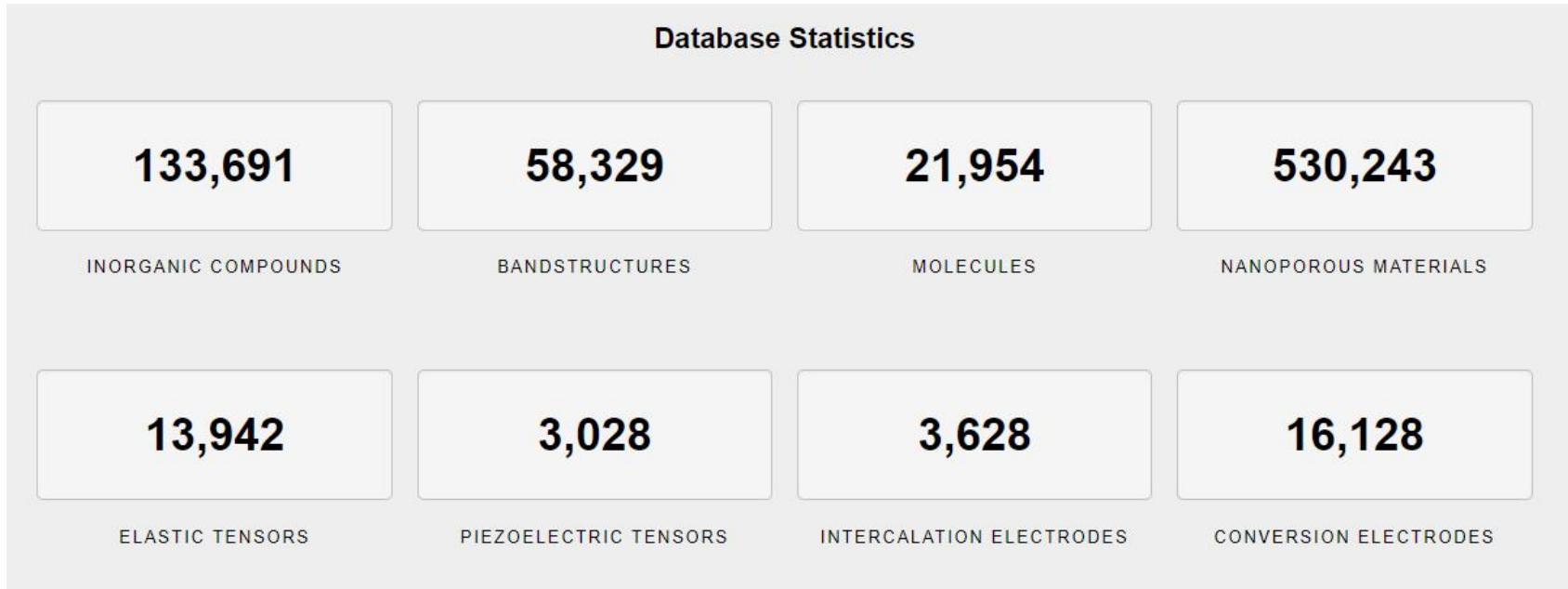
### **bandstructure**

The calculated "line mode" band structure (along selected symmetry lines -- aka "branches", e.g.  $\Gamma$  to  $Z$  -- in the Brillouin zone) in the pymatgen json representation

### **bandstructure\_uniform**

The calculated uniform band structure in the pymatgen json representation

# 材料领域的机器学习



材料基本信息数据已经整理到mp\_index.xlsx文件，供大家参考

# 材料领域的机器学习

The screenshot shows the homepage of the Crystallography Open Database (COD). At the top left is the COD logo, which consists of three stylized spheres colored cyan, lime green, and magenta, with the letters 'C', 'O', and 'D' respectively. To the right of the logo is the text 'Crystallography Open Database'. On the left side of the page is a sidebar with several menu items:

- COD Home**
  - Home
  - What's new?
- Accessing COD Data**
  - Browse
  - Search
  - Search by structural formula
- Add Your Data**
  - Deposit your data
  - Manage depositions
  - Manage/release prepublications
- Documentation**
  - COD Wiki
  - Obtaining COD
  - Querying COD
  - Citing COD
  - COD Mirrors
  - Advice to donators
  - Useful links

In the center of the page, there is a large image of the COD logo. Below it is a descriptive text:  
**Open-access collection of crystal structures of organic, inorganic, metal-organics compounds and minerals, excluding biopolymers.**  
Including data and software from CrystalEye, developed by Nick Day at the department of Chemistry, the University of Cambridge under supervision of Peter Murray-Rust.

All data on this site have been placed in the public domain by the contributors.

Currently there are **405557** entries in the COD.  
Latest deposited structure: [2242911](#) on **2019-04-24 at 02:30:59 UTC**

Crystallography Open Database拥有约40万种晶体结构。

优点：材料数量庞大、提供多种下载方式、免费、API完备、提供材料的文献出处

缺点：缺乏材料的非结构信息

# 材料领域的机器学习



> 199,000 crystal structures

> 160,000  
experimental  
structures

> 10,000  
theoretical  
structures

~30,000  
derived  
structures

> 9,000  
Structure  
types

> 60,000  
authors

> 80,000  
articles

> 1,500  
journals

ICSD拥有接近20万种无机晶体结构及相关的电子结构信息。

优点：晶体结构主要来自实验数据；学术界认可度比较高；搜索方式多样。

缺点：昂贵，无永久license；只有结构数据，没有物理性质。

[http://www2.fiz-karlsruhe.de/icsd\\_home.html](http://www2.fiz-karlsruhe.de/icsd_home.html)

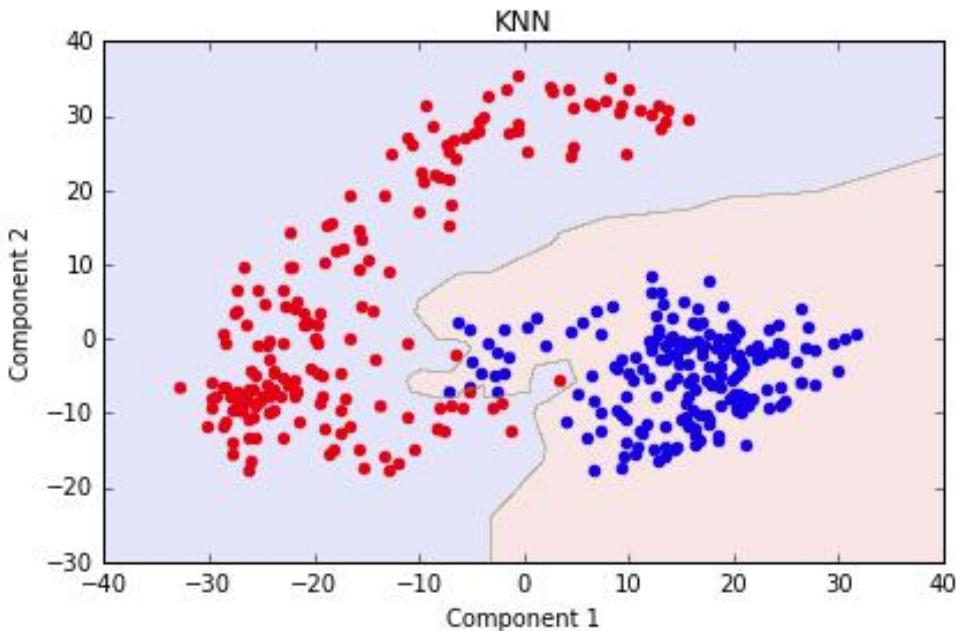
# 材料领域的机器学习

## 常用的分类算法

缩写	全称	线性
KNN	K-nearest neighbors	nonlinear
LogReg	Logistic regression	linear
LDA	Linear discriminant analysis	linear
DT	Decision tree	nonlinear
SVM	Supporting vector machine	Linear or nonlinear

# 材料领域的机器学习

## 常用的分类算法--KNN



根据最近邻的K个点的类别来  
判断“新来的”点归为哪一类  
。

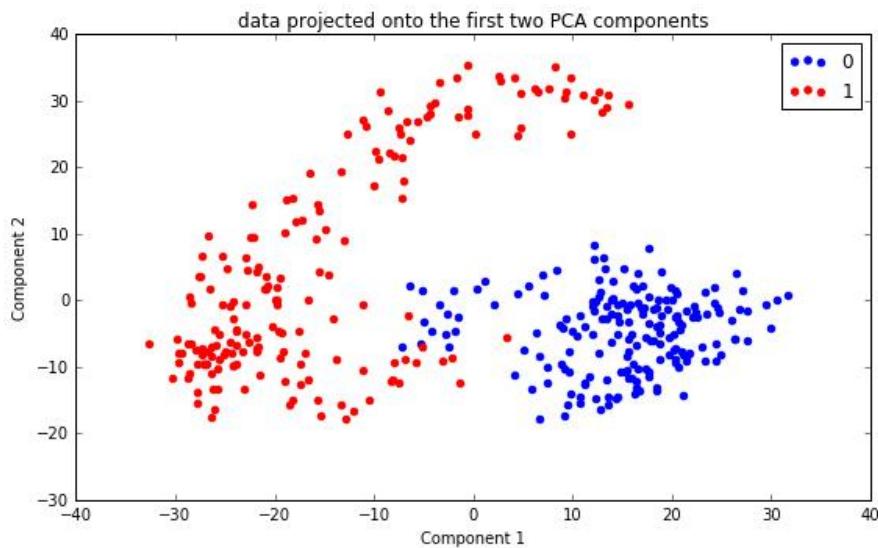
如对于某个新点， $K=5$ 时，其  
最近邻的5个点里3红2蓝，那么  
归为红点。

特点：易于理解和实现；点数  
量多时计算距离耗时；距离的  
定义； $K$ 如何选取

KNN: 近朱者赤，近墨者黑！

# 材料领域的机器学习

## 常用的分类算法--LogReg



LogReg: 名为逻辑回归，其实是分类算法

根据点的分量的线性组合结果，来给出每个点被判为红（蓝）点的概率。如果模型对训练集里点的概率判得不准，则施加惩罚，迫使模型继续调整。

$$\max_{\{\beta_0, \beta_1, \beta_2\}} \ell$$

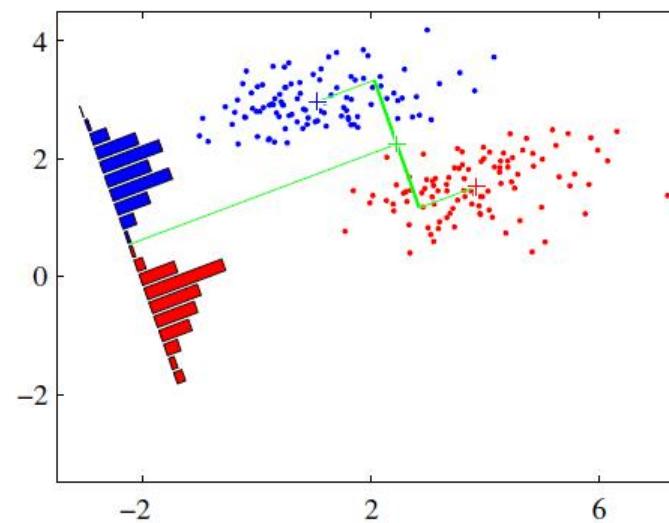
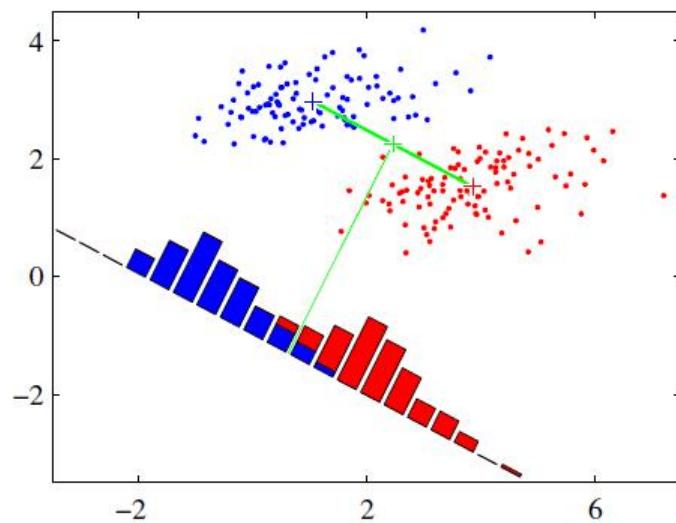
$$\ell \equiv \prod_{y_i=1} p(x_i) \prod_{y_j=0} (1 - p(x_j))$$

$$p(x) = \frac{e^{\beta_0 + \beta_1 x_1 + \beta_2 x_2}}{1 + e^{\beta_0 + \beta_1 x_1 + \beta_2 x_2}}$$

# 材料领域的机器学习

## 常用的分类算法—线性判别分析LDA

LDA将数据在低维度上进行投影，投影后希望每一种类别数据的投影点尽可能的接近，而不同类别的数据的类别中心之间的距离尽可能的大。



LDA可以用于分类也可以用于降维

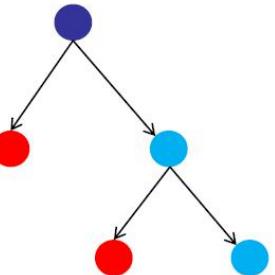
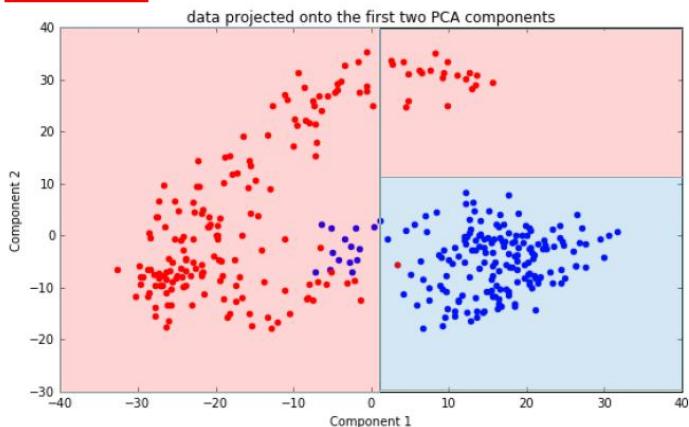
# 材料领域的机器学习

## 常用的分类算法—决策树

Entropy       $S = - \sum_{k=1}^K p_k \ln p_k \quad \sum_{k=1}^K p_k = 1$

Entropy gain       $\Delta S = S - \left( \frac{N_1}{N_1 + N_2} S_1 + \frac{N_2}{N_1 + N_2} S_2 \right)$

max  $\Delta S$



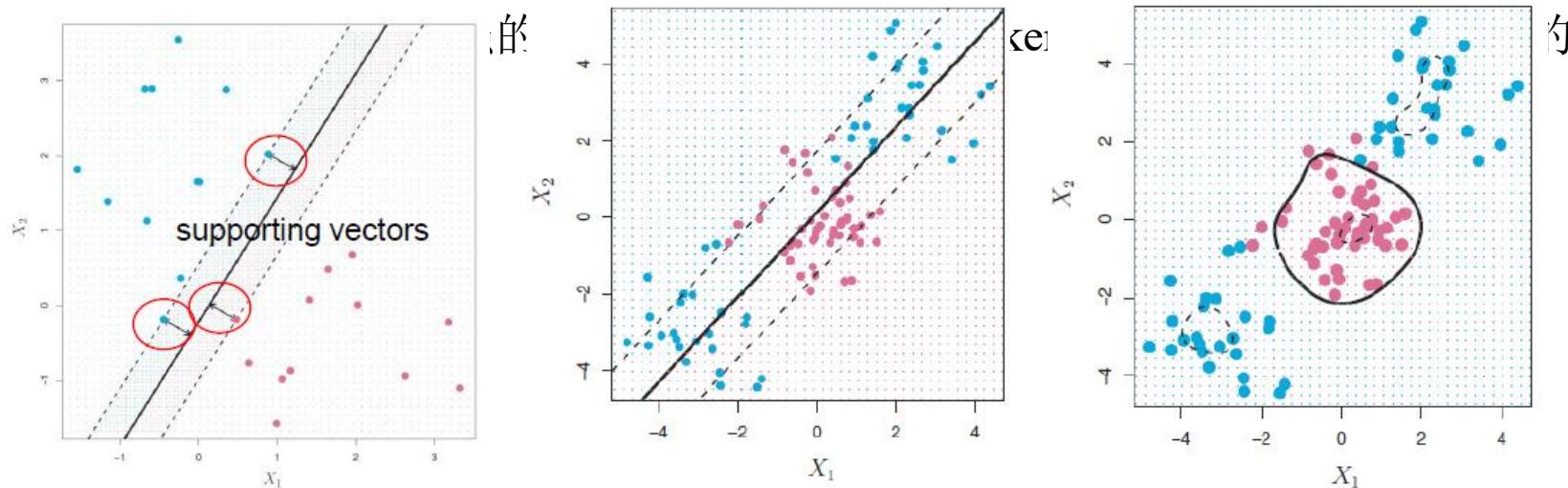
决策树有点像一系列if()语句，通过特征分割来使得信息增益最大。

信息熵有这样的特点：各状态的概率越接近，熵越大，概率越悬殊，熵越小。那么如果分割出的集合里分布越悬殊，熵越小，分割前和分割后的信息增量（“熵增”）越大。

# 材料领域的机器学习

## 常用的分类算法—SVM

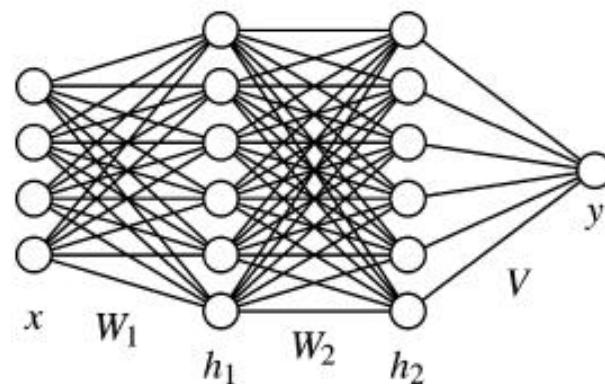
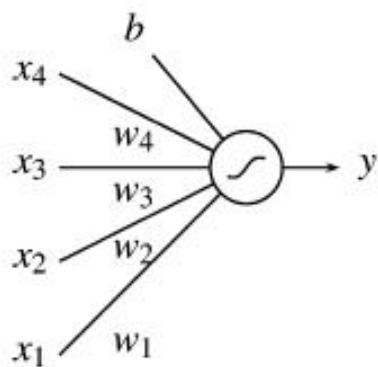
SVM采用超平面(hyper plane)来划分数据点，使得离超平面最近的点尽可能远(最大间隔)。



# 材料领域的机器学习

## 常用的分类算法—神经网络

神经网络是一种多层结构的模型，每一层由多个特征组成，每个特征与前一层的若干特征相连，即线性组合及非线性激活。



<http://playground.tensorflow.org>

# 材料领域的机器学习

## 模型选择---交叉验证

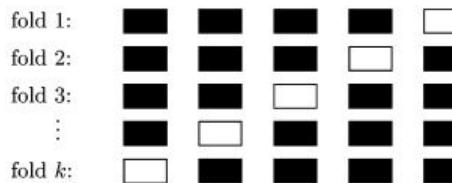
为了更准确地评估模型的有效性，可以采用交叉验证(cross-validation)的方法。

K-交叉验证从训练集里拆成K份，每次选一份用于验证评估，其余用于训练，综合K次评估结果得到模型的成绩。

1. Split data into  $k$  sets of roughly the same size, e.g. into  $k = 5$  splits.
2. Use  $(k - 1)$  splits for training and model selection. Then test the generated model on the remaining hold-out or test split.



3. Repeat step 2.  $k$ -times, i.e. until each subset has been once used for testing.

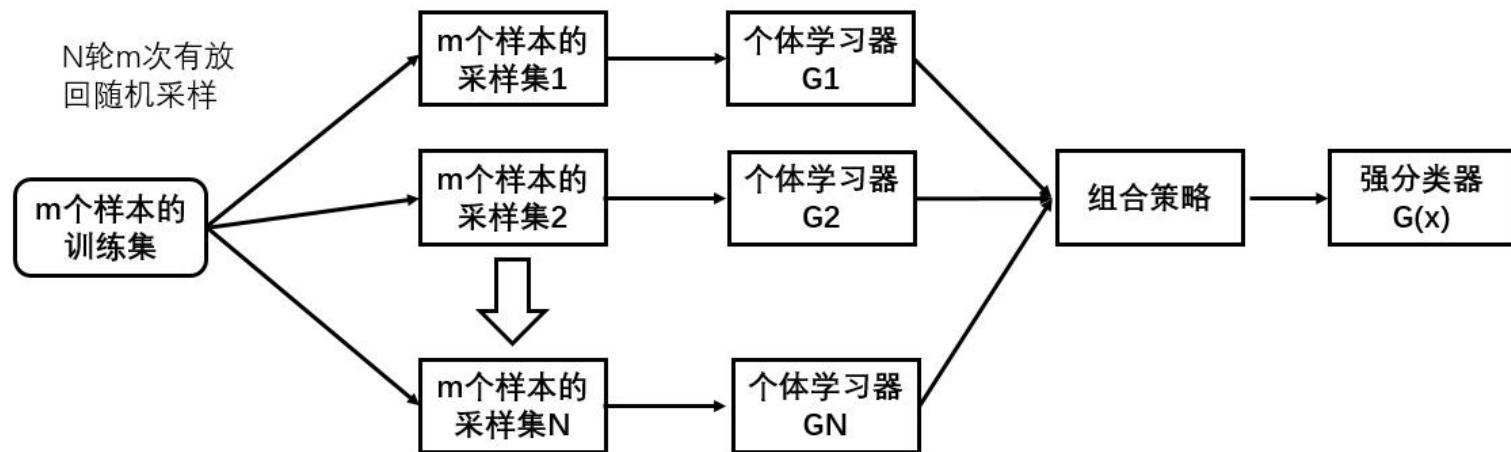


4. Combine the  $k$  estimates of the prediction error into one cross-validation error.

# 材料领域的机器学习

## 模型选择---bagging

通过捆绑组合多个模型（学习器）的方式，提高整体的鲁棒性（Robustness），准确程度。除了bagging外还有boost等方法。



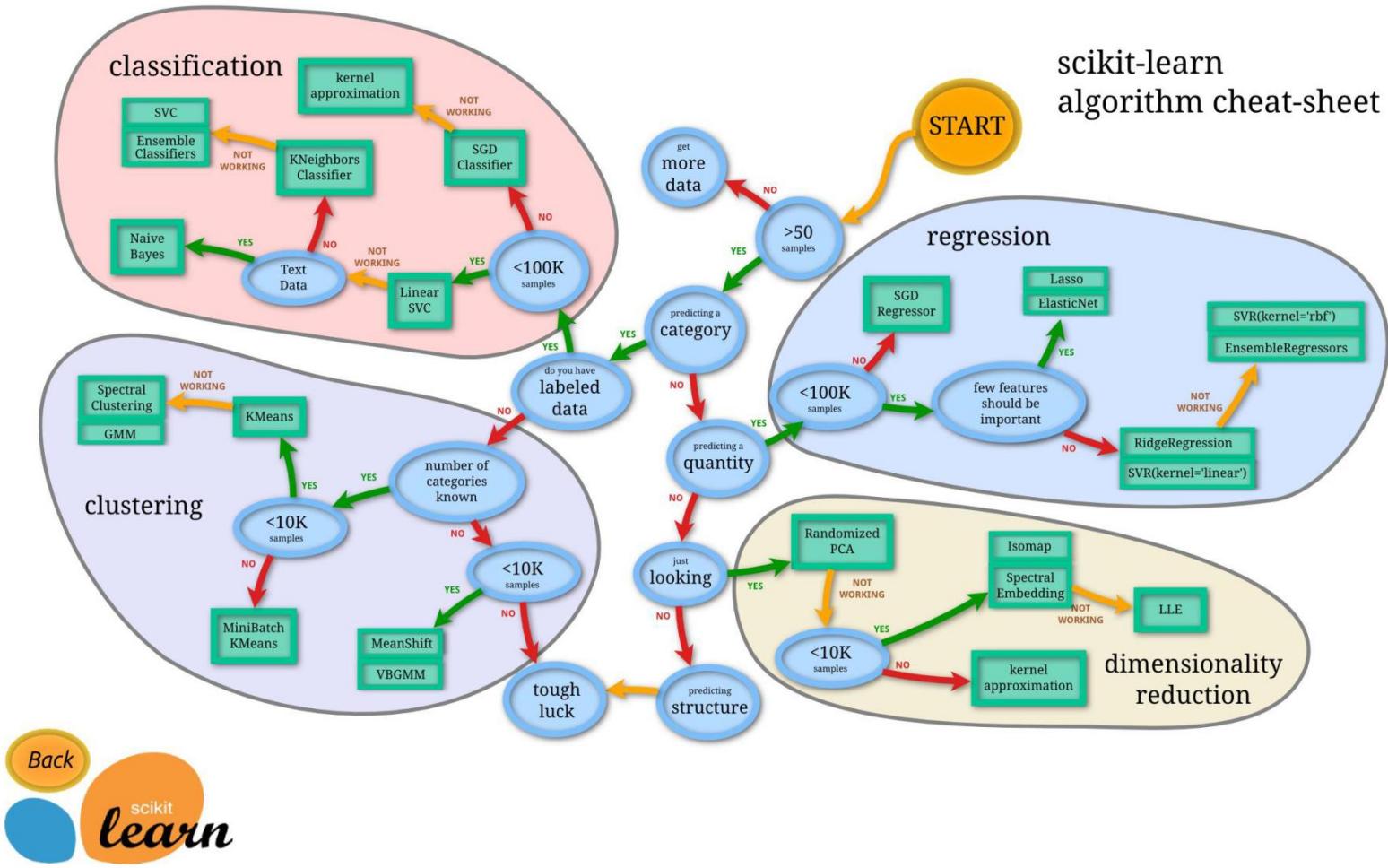
# Python里常用的机器学习、材料学相关库

## 经典的机器学习库scikit-learn



支持**分类、回归、聚类、降维、模型选择、数据预处理**等多类型任务。封装程度很高，易于使用。

# Machine learning algorithms

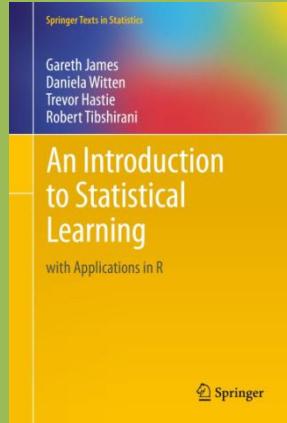


# Machine learning algorithms



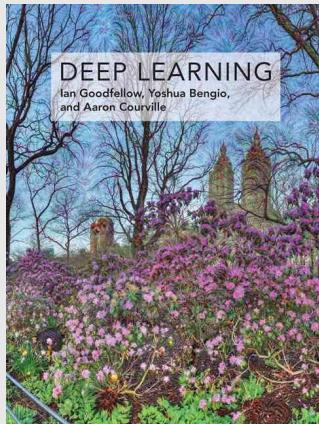
# Data analysis tools

Statistical Learning



$10^2$  to  $10^3$  data points  
physics interpretation

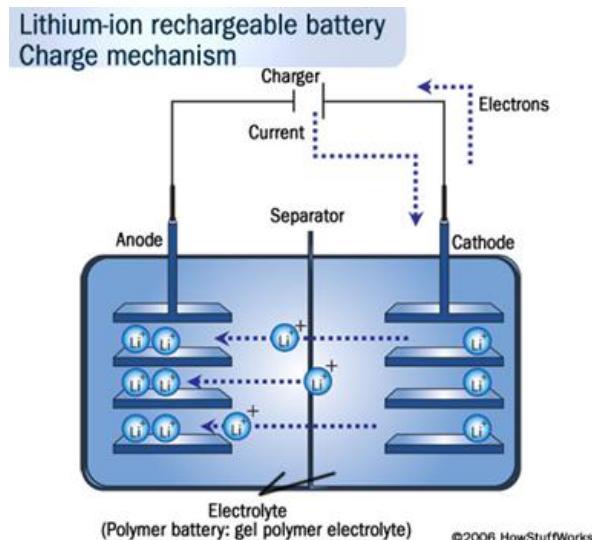
Deep Learning



$> 10^4$  data points  
large model capacity

# 固态锂离子导体材料的虚拟筛选

## 固态锂离子导体材料



大多数锂电池里，电解质是液态的，即锂离子盐溶解在有机溶剂里。

优点：廉价，高的锂离子电导率

缺点：安全问题如机械穿刺引起的短路，发热导致压力增大等

如何寻找固态的锂离子导体材料？

Guess-and-check? 花费了数十年，仅得到了数十种

# Knowledge

- The size of training set is relatively small in materials science
- Human knowledge can help design effective descriptors

Energy &  
Environmental  
Science



PAPER

[View Article Online](#)  
[View Journal](#)



Cite this: DOI: 10.1039/c6ee02697d

Holistic computational structure screening of  
more than 12 000 candidates for solid lithium-ion  
conductor materials†

Austin D. Sendek,<sup>a</sup> Qian Yang,<sup>b</sup> Ekin D. Cubuk,<sup>c</sup> Karel-Alexander N. Duerloo,<sup>c</sup>  
Yi Cui<sup>c</sup> and Evan J. Reed<sup>\*c</sup>

Material Project里含有约12000种含锂的晶体结构，很可能存在“沉睡的”优秀目标材料。如何找到它们？

# Solid lithium-ion conductors

66,840 candidates



containing Li atoms

12,831 candidates



band gap, anti-oxidization, structural stability, no transition metal, cost, earth abundance

317 candidates



Li conduction: machine learning trained with 40 known materials

21 candidates

# Screening

Requirement	Reasoning	Filter
Electronic conductivity	$\sigma = (\mu_e + \mu_h)q\sqrt{N_C N_V} e^{-E_g/2kT}$	$E_g > 1eV$
Structure stability	Energy above hull: The decomposition energy of this material into the set of most stable materials	$E_{hull} = 0$
Stability vs. oxidation at cathode	$Li_x A_a B_b C_c \xrightarrow{\Delta G_f} xLi^0 + aA^0 + bB^0 + cC^0$	$\tilde{V}_{ox} \equiv \Delta G_f / xF$ $\tilde{V}_{ox} > 4V$
Stability vs. reduction at anode	Transition metals have many stable oxidation states	No transition metal

# 固态锂离子导体材料的虚拟筛选

## 机器学习描述符筛选---训练集的准备

从文献中搜集了40种有离子电导率的含Li材料，其中高离子电导率的11种。

晶体结构从ICSD种下载。

$$\tilde{\sigma} = \begin{cases} 1, \sigma \geq 10^{-4} \text{ S cm}^{-1} \\ 0, \sigma < 10^{-4} \text{ S cm}^{-1} \end{cases}$$

Composition	RT bulk ionic conductivity ( $\text{S cm}^{-1}$ )	Ionic conductivity ref.	Structure ref.
$\text{LiLa}(\text{TiO}_3)_2$	$1 \times 10^{-3}$	17	29
$\text{Li}_{9.81}\text{Sn}_{0.81}\text{P}_{2.19}\text{S}_{12}$	$5.5 \times 10^{-3}$	30	30
$\text{Li}_{10}\text{Ge}(\text{PS}_6)_2$	$1.4 \times 10^{-2}$	7	31
$\text{Li}_{10.35}\text{Si}_{1.35}\text{P}_{1.65}\text{S}_{12}$	$6.5 \times 10^{-3}$	30	30
$\text{Li}_{14}\text{ZnGe}_4\text{O}_{16}(2)$	$1.0 \times 10^{-6}$	32	33 and 34
$\text{Li}_2\text{Ca}(\text{NH})_2$	$6.4 \times 10^{-6}$	35	36
$\text{Li}_2\text{Ge}_7\text{O}_{15}$	$5.0 \times 10^{-6}$	37	38
$\text{Li}_2\text{NH}$	$2.5 \times 10^{-4}$	35	39
$\text{Li}_2\text{S}$	$1.0 \times 10^{-13}$	40	41
$\text{Li}_{13.6}\text{Si}_{2.8}\text{S}_{1.2}\text{O}_{16}$	$6.0 \times 10^{-7}$	42	43
$\text{Li}_{14}\text{Ge}_2\text{V}_2\text{O}_{16}$	$7.0 \times 10^{-5}$	44	45

# 固态锂离子导体材料的虚拟筛选

## 机器学习描述符筛选---20个Li相关描述符

Feature	Pearson correlation coefficient
1 Volume per atom <sup>a</sup>	0.20
2 Standard deviation in Li neighbour count	0.22
3 Standard deviation in Li bond ionicity	-0.04
4 Li bond ionicity <sup>a</sup>	-0.18
5 Li neighbour count <sup>a</sup>	-0.19
6 <i>Li-Li bonds per Li</i> <sup>a</sup>	0.06
7 <i>Bond ionicity of sublattice</i> <sup>a</sup>	-0.28
8 Sublattice neighbour count <sup>a</sup>	-0.13
9 Anion framework coordination <sup>a</sup>	-0.06
10 Minimum anion-anion separation distance <sup>a</sup> (Å)	0.09
11 Volume per anion (Å <sup>3</sup> )	-0.01
12 Minimum Li-anion separation distance <sup>a</sup> (Å)	0.20
13 Minimum Li-Li separation distance <sup>a</sup> (Å)	-0.10
14 Electronegativity of sublattice <sup>a</sup>	-0.16
15 Packing fraction of full crystal	0.16
16 Packing fraction of sublattice	0.19
17 Straight-line path width <sup>a</sup> (Å)	0.07
18 Straight-line path electronegativity <sup>a</sup>	-0.29
19 Ratio of features (4) and (7)	-0.03
20 Ratio of features (5) and (8)	-0.18
Constant term	—

20个描述符与离子电导率的相关系数都很低。单独使用是不合适的。

解决方案---把低相关度的描述符组合成高相关度特征！

$$P_{LR} \left( \tilde{\sigma}^{(i)} = 1 \right) = \left[ 1 + \exp \left( - \sum_{j=0}^n \theta_j x_j^{(i)} \right) \right]^{-1}$$

PLR > 50%，则把材料判为1类  
(高离子电导率)

PLR < 50%，则判为0类。

# Features design

**Features design relies on professional knowledge to identify the most relevant factors**

---

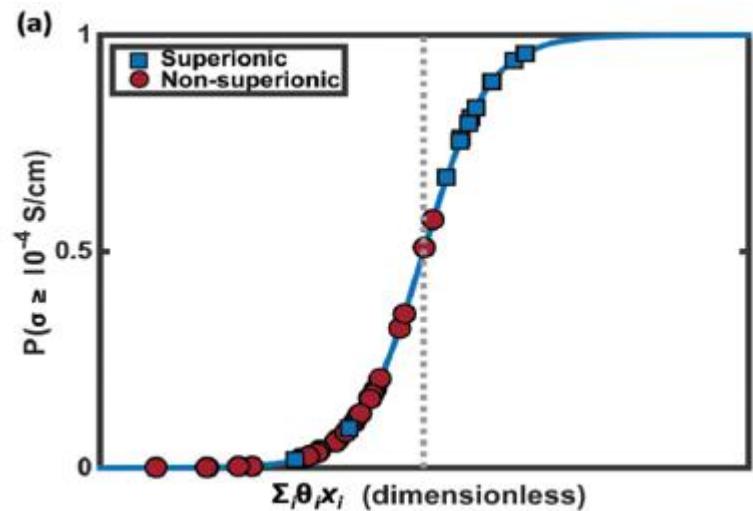
Features	Definition
LLB	The average number of Li neighbors for each Li
SBI	The average sublattice bond iconicity
AFC	The average anion-anion coordination number in the anion framework
LASD	The average shortest Li-anion distance in angstroms
LSSD	The average shortest Li-Li distance in angstroms

# Ionic conductivity screening

$P(x) > 0.5$  good ionic conductor  
 $P(x) < 0.5$  bad ionic conductor

$$P(x) \equiv \frac{\exp(\sum_i \theta_i x_i)}{1 + \exp(\sum_i \theta_i x_i)}$$

$$\begin{aligned} \sum_i \theta_i x_i = & 0.184 \times LLB - 4.009 \times SBI - 0.467 \times AFC \\ & + 8.699 \times LASD - 2.17 \times LLSD - 6.564 \end{aligned}$$



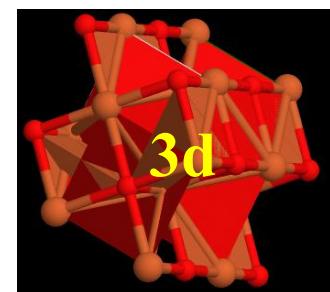
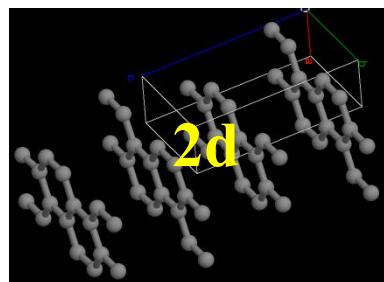
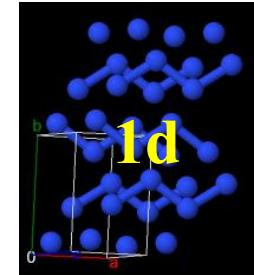
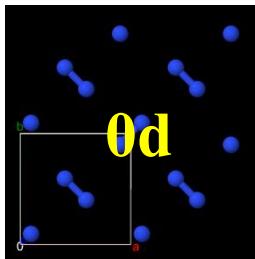
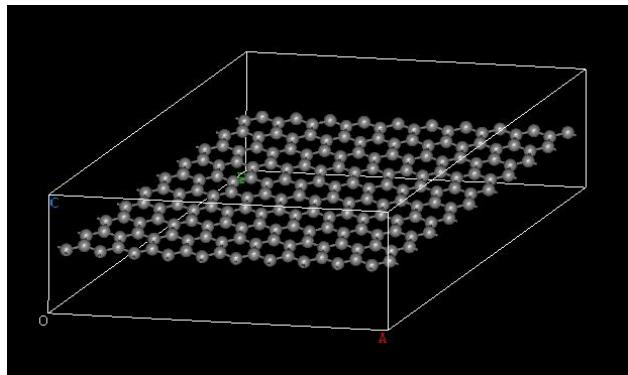
Logistic regression

# 训练结果

MPIID	Chemical formula
mp-554076	BaLiBS <sub>3</sub>
mp-532413	Li <sub>5</sub> B <sub>7</sub> S <sub>13</sub>
mp-569782 <sup>a</sup>	Sr <sub>2</sub> LiCBr <sub>3</sub> N <sub>2</sub>
mp-558219	SrLi(BS <sub>2</sub> ) <sub>3</sub>
mp-15797	LiErSe <sub>2</sub>
mp-29410	Li <sub>2</sub> B <sub>2</sub> S <sub>5</sub>
mp-676361	Li <sub>3</sub> ErCl <sub>6</sub>
mp-643069 <sup>a</sup>	Li <sub>2</sub> HIO
mp-19896	Li <sub>2</sub> GePbS <sub>4</sub>
mp-7744 <sup>a</sup>	LiSO <sub>3</sub> F
mp-22905 <sup>b</sup>	LiCl
mp-34477	LiSmS <sub>2</sub>
mp-676109	Li <sub>3</sub> InCl <sub>6</sub>
mp-559238	CsLi <sub>2</sub> BS <sub>3</sub>
mp-866665 <sup>a</sup>	LiMgB <sub>3</sub> (H <sub>9</sub> N) <sub>2</sub>
mp-8751	RbLiS
mp-15789	LiDyS <sub>2</sub>
mp-15790	LiHoS <sub>2</sub>
mp-15791	LiErS <sub>2</sub>
mp-561095 <sup>a</sup>	LiHo <sub>3</sub> Ge <sub>2</sub> (O <sub>4</sub> F) <sub>2</sub>
mp-8430	KLiS

# 二维铁磁材料的虚拟筛选

## 二维材料



如何用尽可能低的成本从材料数据库里把二维材料找出来？

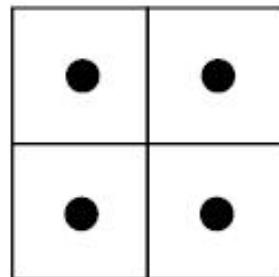
# 二维铁磁材料的虚拟筛选

## 二维材料—维度描述符

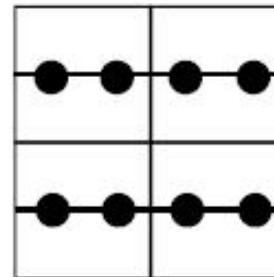
扩晶胞，计算连接的原子数量，  
对比值求2的对数。

$$2^d = \frac{N_{2 \times 2 \times 2}}{N_{1 \times 1 \times 1}}.$$

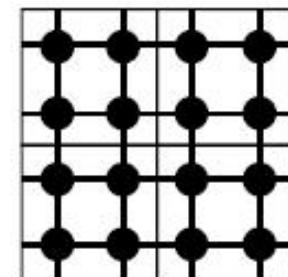
0d



1d



2d



$$D_{12} < R_1 + R_2 + \delta R,$$

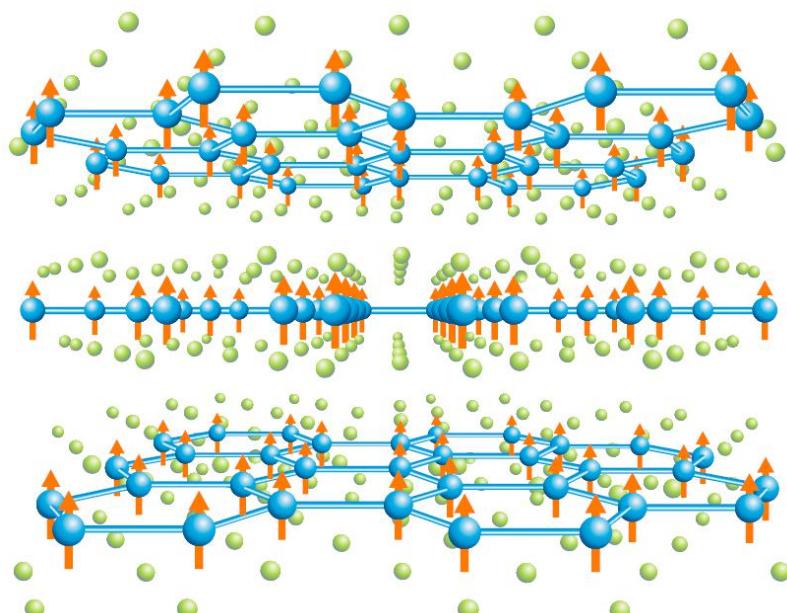
# 二维铁磁材料的虚拟筛选

dimensionality	dR = 0.5	dR = 1.0	dR = 1.5
0d	3,506	1,839	910
1d	1,257	867	577
2d	3,531	2,510	1,802
3d	59,188	62,266	64,194

通过简单的1个描述符，马上找到了数据库里全部2d材料。调控dR可以提高维度描述符的严格程度。

# Two recent experiments

Ferromagnetism was found in 2d materials experimentally



## LETTER

doi:10.1038/nature22060

### Discovery of intrinsic ferromagnetism in two-dimensional van der Waals crystals

Cheng Gong<sup>1\*</sup>, Lin Li<sup>2\*</sup>, Zhenglu Li<sup>3,4\*</sup>, Huiwen Ji<sup>5</sup>, Alex Stern<sup>2</sup>, Yang Xia<sup>1</sup>, Ting Cao<sup>3,4</sup>, Wei Bao<sup>1</sup>, Chenzhe Wang<sup>1</sup>, Yuan Wang<sup>1,4</sup>, Z. Q. Qiu<sup>3</sup>, R. J. Cava<sup>5</sup>, Steven G. Louie<sup>3,4</sup>, Jing Xia<sup>2</sup> & Xiang Zhang<sup>1,4</sup>

## LETTER

doi:10.1038/nature22391

### Layer-dependent ferromagnetism in a van der Waals crystal down to the monolayer limit

Bevin Huang<sup>1\*</sup>, Genevieve Clark<sup>2\*</sup>, Efrén Navarro-Moratalla<sup>3\*</sup>, Dahlia R. Klein<sup>3</sup>, Ran Cheng<sup>4</sup>, Kyle L. Seyler<sup>1</sup>, Ding Zhong<sup>1</sup>, Emma Schmidgall<sup>1</sup>, Michael A. McGuire<sup>5</sup>, David H. Cobden<sup>1</sup>, Wang Yao<sup>6</sup>, Di Xiao<sup>4</sup>, Pablo Jarillo-Herrero<sup>3</sup> & Xiaodong Xu<sup>1,2</sup>

UC-Berkeley group	$\text{Cr}_2\text{Ge}_2\text{Te}_6$
UW and MIT group	$\text{CrI}_3$

# Pre-screening for 2d ferromagnetic materials

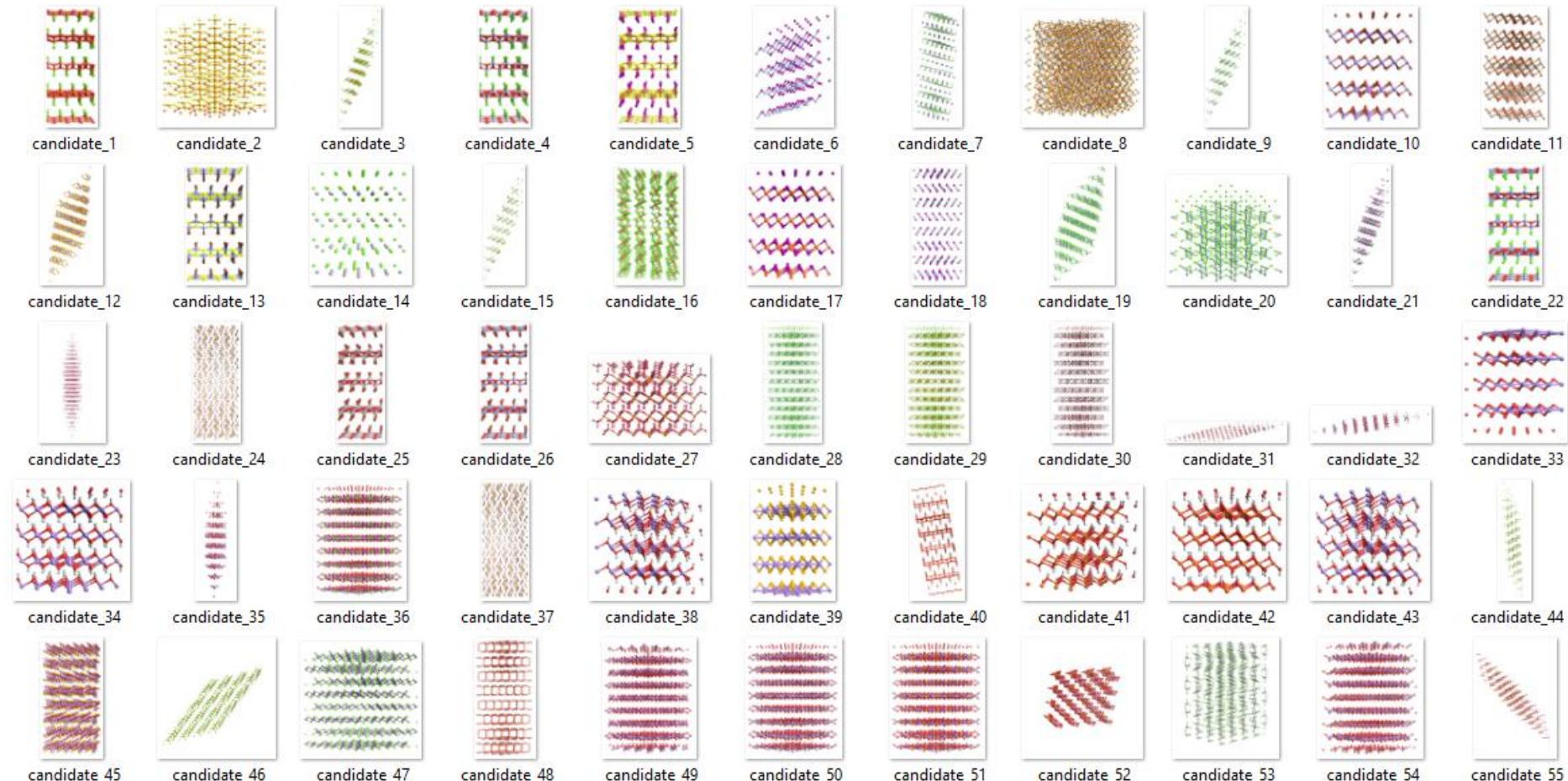
Goal: Search for materials with layered structure and ferromagnetism

## Pre-screening criterion

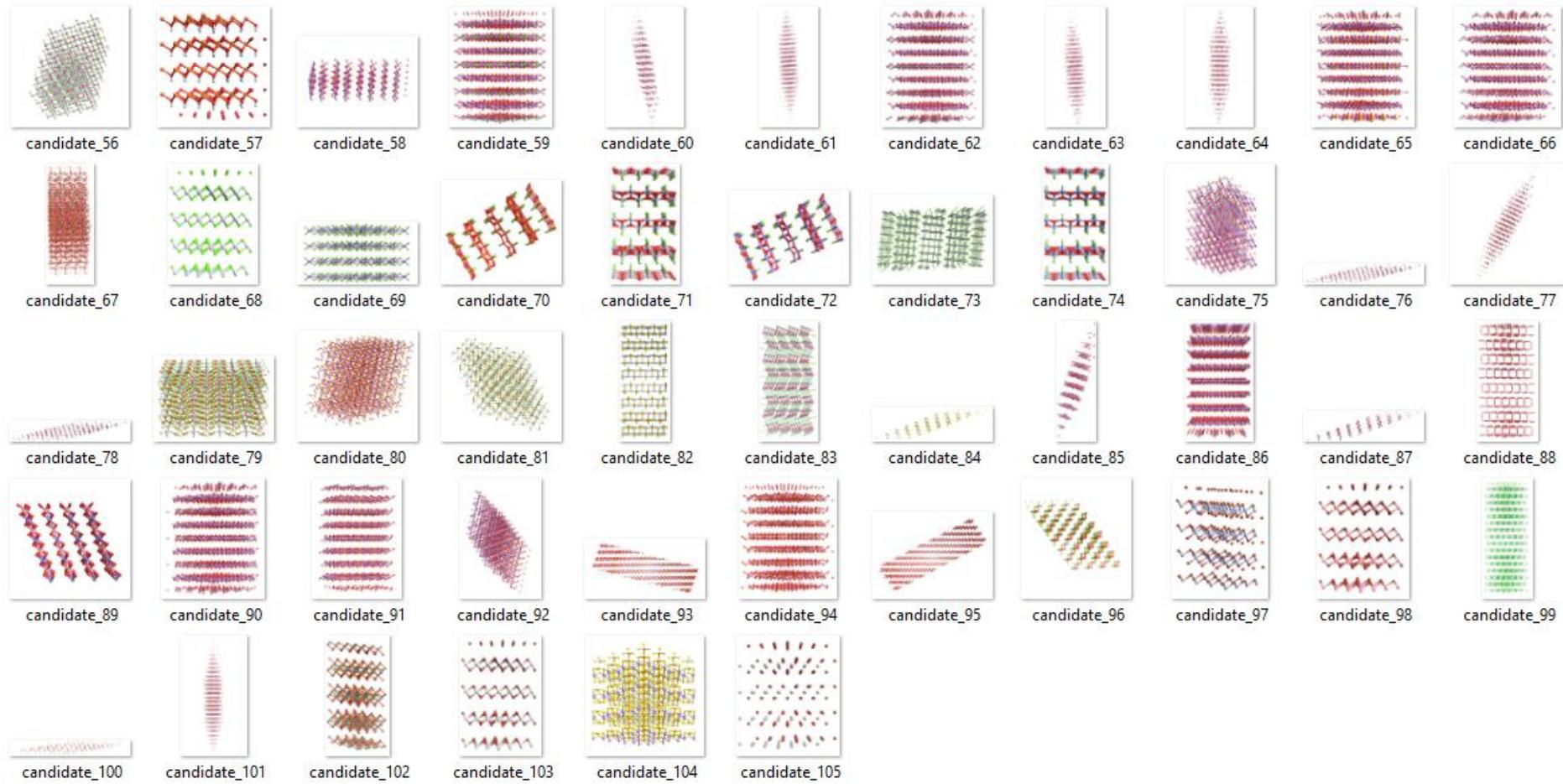
- 1) Material existed (use ICSD)
- 2) dimension = 2
- 3) packing factor < 0.354
- 4) magnetic moment per atom > 0.625 m<sub>B</sub>
- 5) Energy above hull < 0.136 eV

materials	mp-id	quantity
diamond	mp-66	$\delta E = 0.136$
graphite	mp-568286	$p = 0.143$
MoS <sub>2</sub>	mp-1434	$p = 0.354$
Fe	mp-13	$\mu = 2.332$
Co	mp-54	$\mu = 3.319$
Ni	mp-23	$\mu = 0.625$

# Results: 105 candidates out of 187,093 compounds (1-55)



# Results: 105 candidates (56-105)



# Rediscover experimental materials

MATERIAL ID: DOI:  
**CrGeTe<sub>3</sub>** **mp-541449** **10.17188/1265115**

[Electronic Structure](#) [X-Ray Diffraction](#) [Substrates](#) [Elasticity](#) [Calculation Summary](#)

HM: P 1  
a=6.913 Å  
b=6.913 Å  
c=21.818 Å  
α=90.000°  
β=90.000°  
γ=120.000°

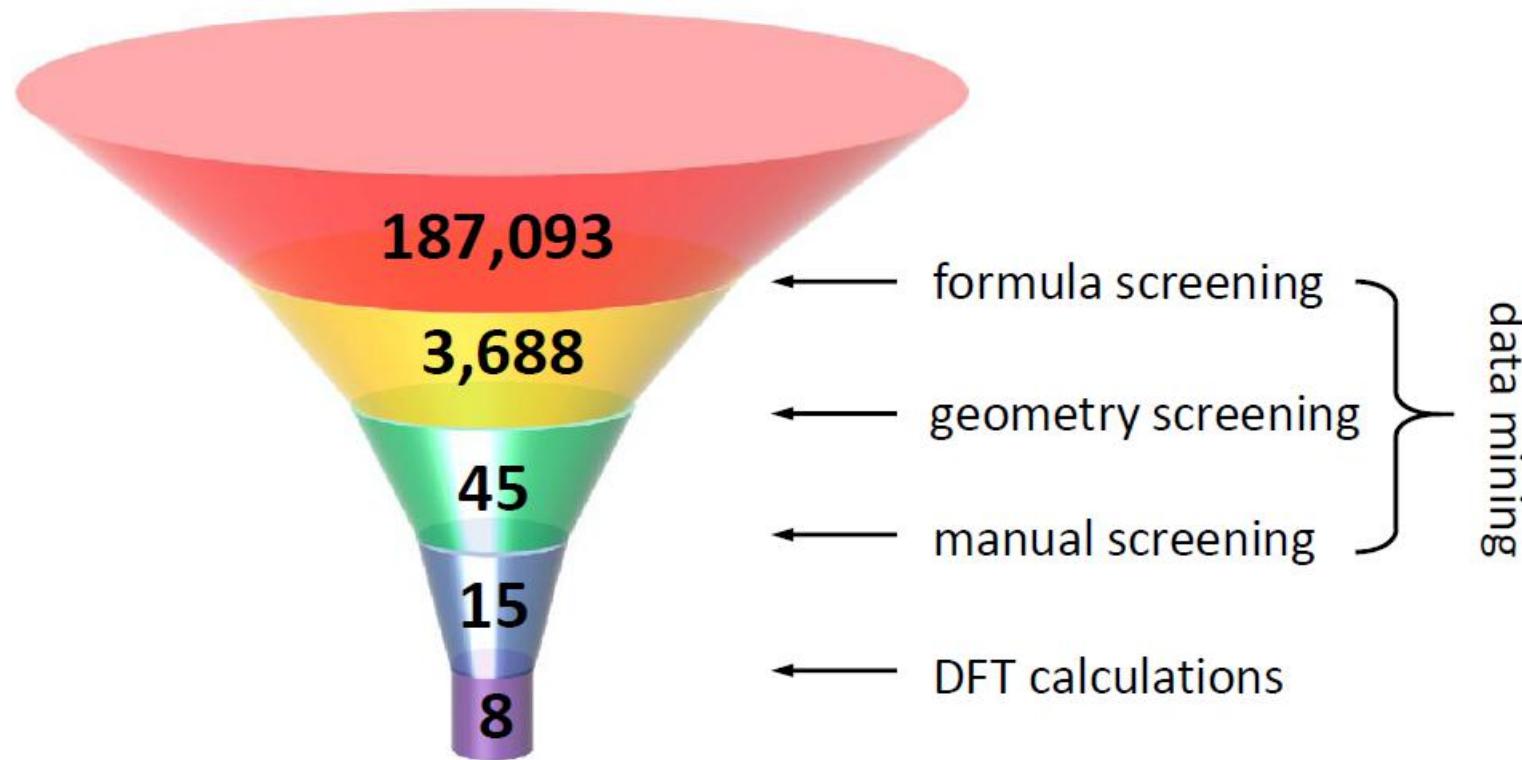
UC group	Cr <sub>2</sub> Ge <sub>2</sub> Te <sub>6</sub>
UW and MIT group	CrI <sub>3</sub>
mp-541449	CrGeTe <sub>3</sub>
mp-27734	CrBr <sub>2</sub>
mp-567504	CrCl <sub>3</sub>

# Add one piece of physics to the search criterion:

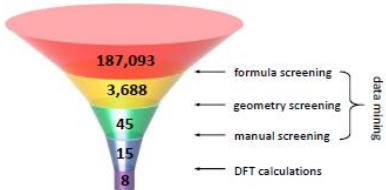
## screening criteria

- 1) Material exists (so use ICSD)
- 2) dimension = 2
- 3) packing factor < 0.354
- 4) magnetic moment per atom > 0.625 m<sub>B</sub>
- 5) Energy above hull < 0.136 eV
- 6) Must have M-Z-M network: M = transition metal atom, Z=heavy atom (Z > 49). This ensures some super-exchange.

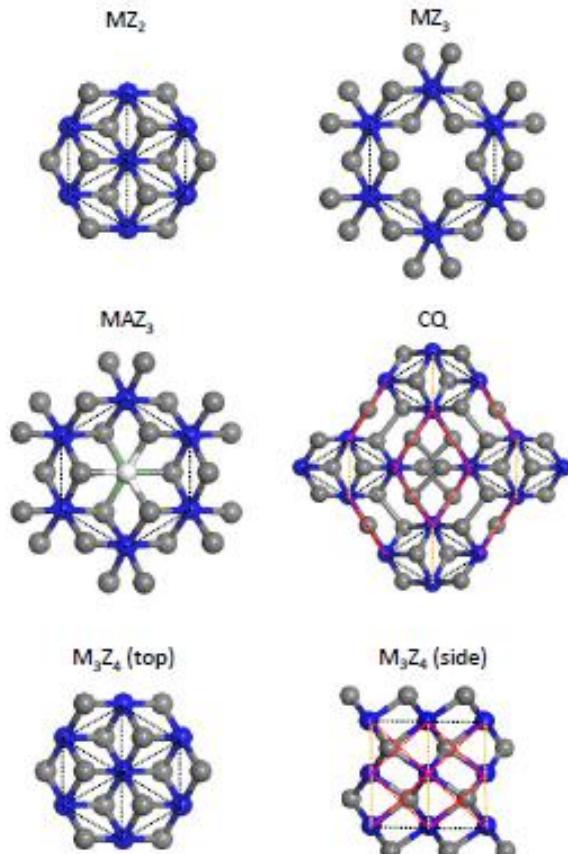
# Mining the ICSD for 2D magnetic materials



Phys. Rev. Mater. 2, 081001(R) (2018)



# DFT and Monte Carlo data

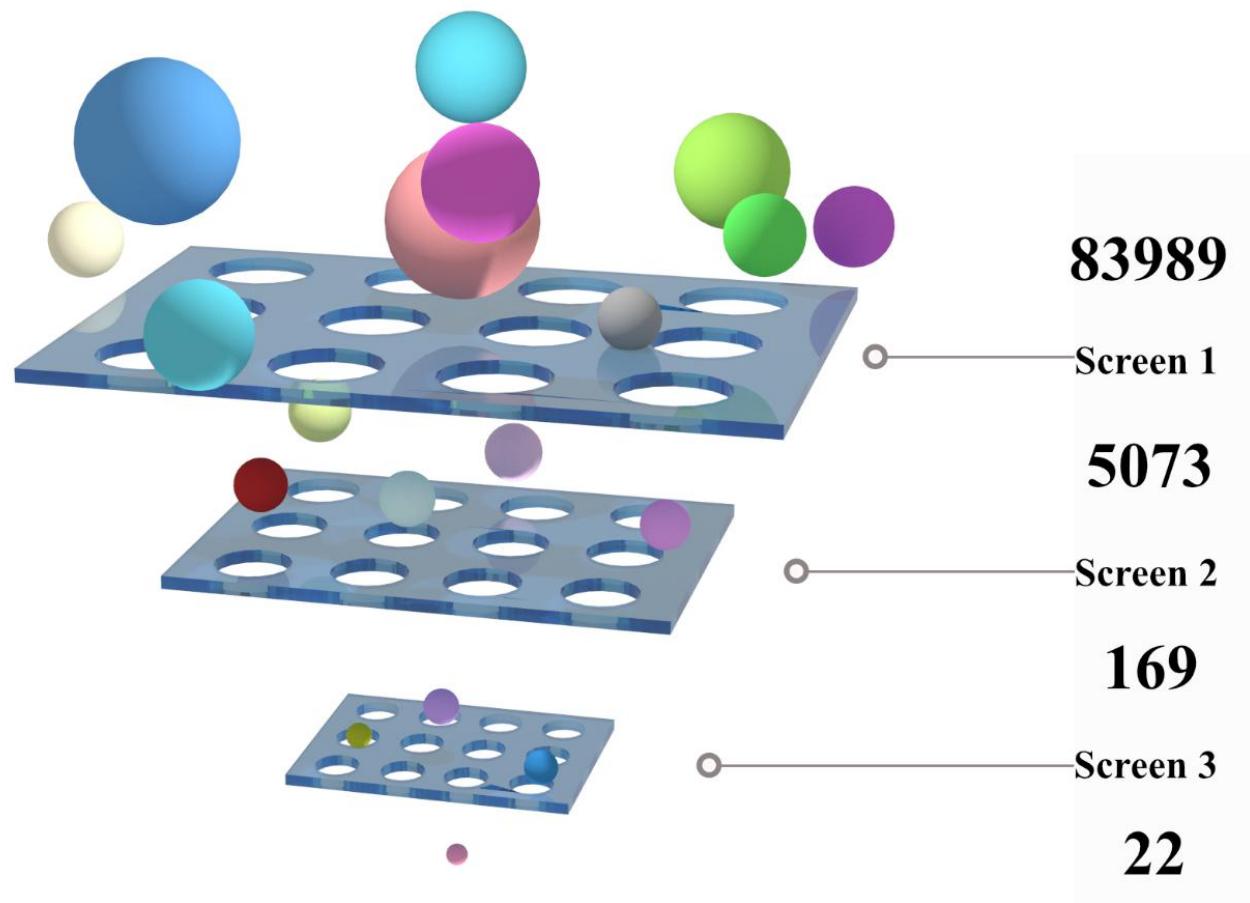


#	ICSD	formula	structure	ordering	J(meV)	T <sub>c</sub> (K)
1	52368	CoI <sub>2</sub>	-	AFM	-	-
2	52369	FeI <sub>2</sub>	-	AFM	-	-
3	33673	MnI <sub>2</sub>	MZ <sub>2</sub>	FM	0.3	15
4	22108	NiI <sub>2</sub>	MZ <sub>2</sub>	FM	1.5	63
5	246907	VI <sub>2</sub>	-	AFM	-	-
6	603582	VTe <sub>2</sub>	MZ <sub>2</sub>	FM	3.0	128
7	626809	CrSiTe <sub>3</sub>	MAZ <sub>3</sub>	FM	12.2	214
8	252343	CrGeTe <sub>3</sub>	MAZ <sub>3</sub>	FM	17.8	314
9	251655	CrI <sub>3</sub>	MZ <sub>3</sub>	FM	9.1	161
10	180602	FeTe	-	AFM	-	-
11	66958	MnCaSn	-	AFM	-	-
12	4073	CrI <sub>2</sub>	-	AFM	-	-
13	76730	NiTe	-	AFM	-	-
14	35266	CrTe <sub>3</sub>	CQ	FM	5.0	71
					16.5	
					1.5	
15	626873	Cr <sub>3</sub> Te <sub>4</sub>	sMZ <sub>2</sub>	FM	16.6	2057
					18.8	
					12.0	

Using the 2 experimental data, get a heuristic scaling factor of T<sub>c</sub>: 0.2 ~ 0.4.

# 搜索光催化材料

- (1) Allowed elements
- (2) ICSD
- (3)  $E_{hull} \leq 0.02$
- (4)  $4 \leq K_{comp} \leq 6$
- (5)  $0 < E_{gap} \leq 3$  eV
- (6) Direct band gap



# 搜索光催化材料

Band edge positions:

$$E_{VB}^0 = \chi(S) - E_e + \frac{1}{2}E_g$$

$$\chi(S) = \sqrt[N]{\chi_1^r \chi_2^s \cdots \chi_{n-1}^p \chi_n^q}$$

[https://github.com/nevbac/photocatalytic-material-searching/tree/master/searching\\_engine](https://github.com/nevbac/photocatalytic-material-searching/tree/master/searching_engine)